



# Controlling underwater sound propagation using 3D-printed phononic crystals

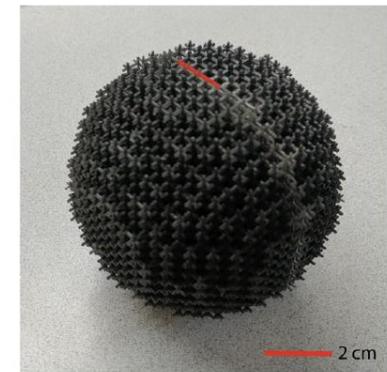
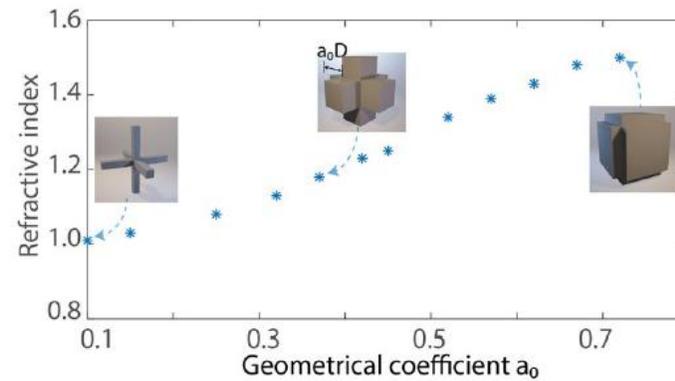
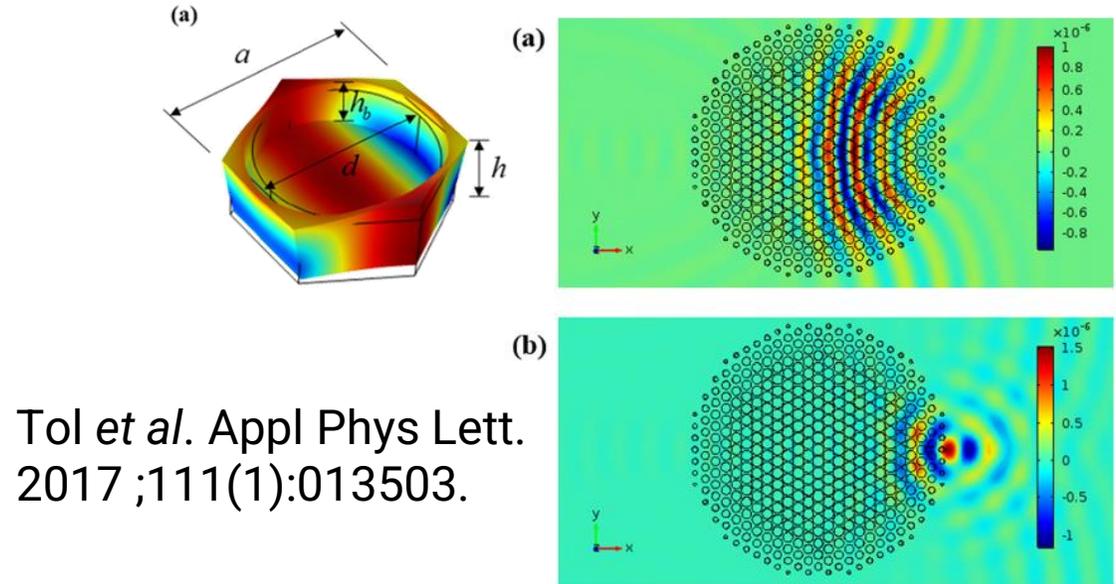
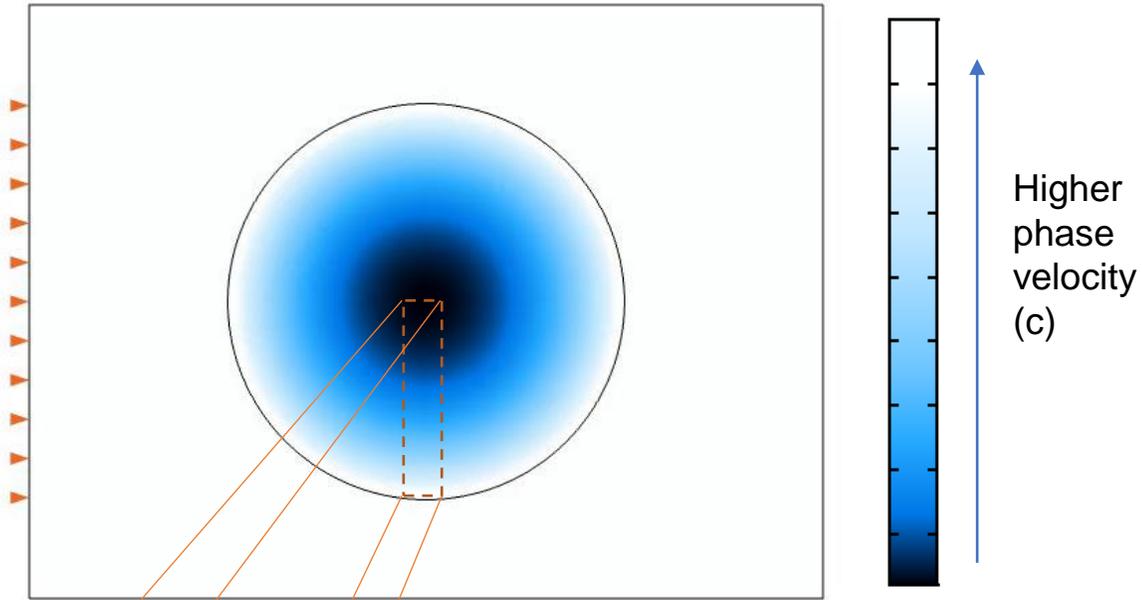
Ahmed Allam, Karim Sabra and Alper Erturk

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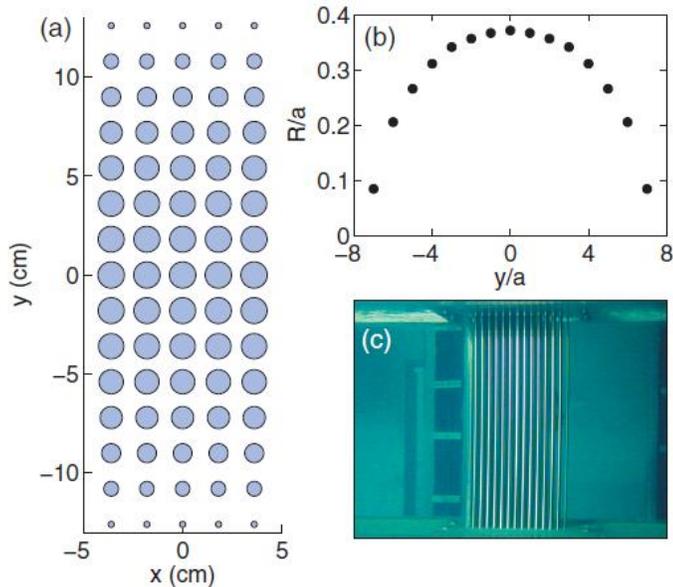
178th meeting, San Diego, California

# Background

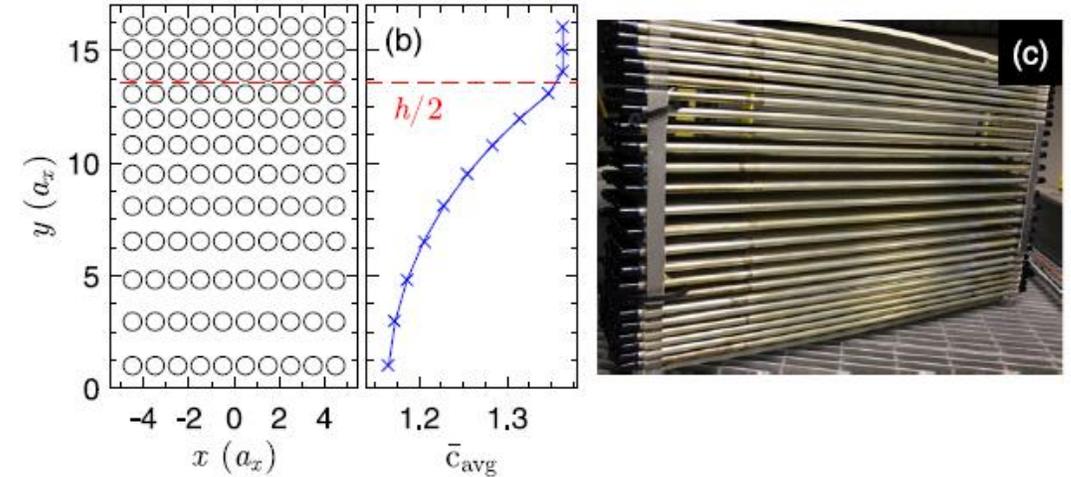


# Underwater implementations

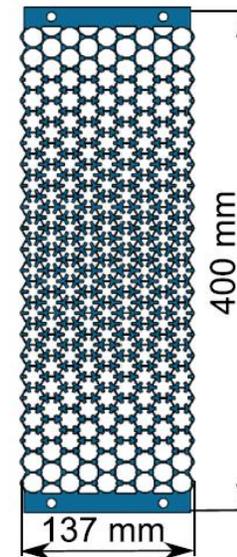
- Use heavy metallic scatterers
- Limited to 2.5D designs
- Difficult to extend to 3D designs due to manufacturing limitations



Martin, T. P. *et al.* *Appl. Phys. Lett.* **97**, 113503 (2010).



Martin, T. P. *et al.* *Phys. Rev. Applied* **4**, 034003 (2015).



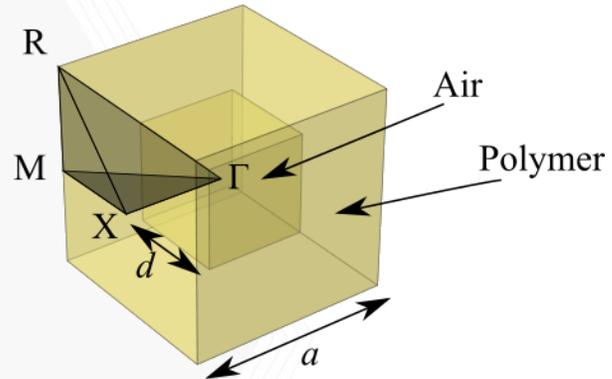
Su, X. *et al.* *J. Acoust. Soc. Am.* **141**, 4408–4417 (2017).

# Objectives

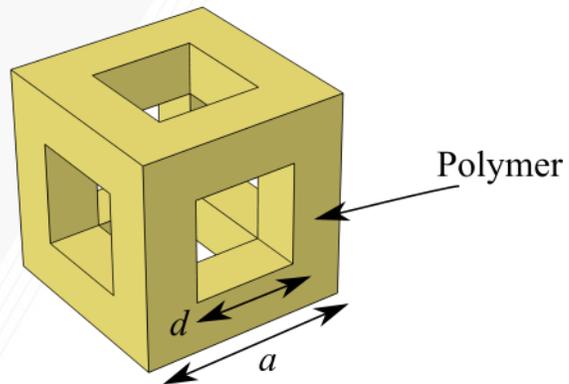
- Design a 3D gradient index phononic crystal capable of achieving a large variation in the effective refractive index compared to water.
- Use this phononic crystal to design a 3D Luneburg lens for focusing underwater acoustic waves.
- Use common 3D printing techniques to manufacture the lens.

# Unit cell design

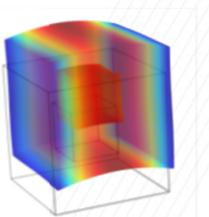
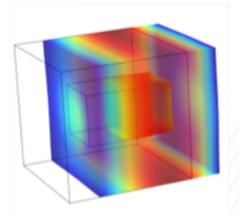
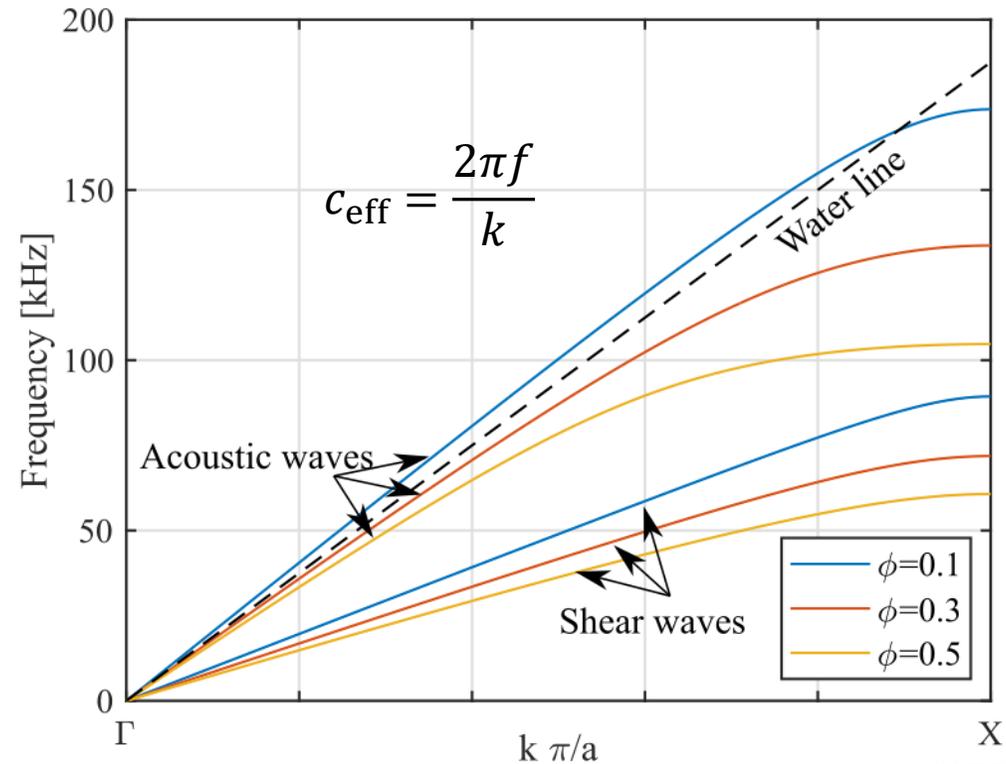
Cell design 1:



Cell design 2:



- Using a Comsol finite-element model of the unit cell is used to estimate the dispersion.



$\phi$ : volume filling fraction

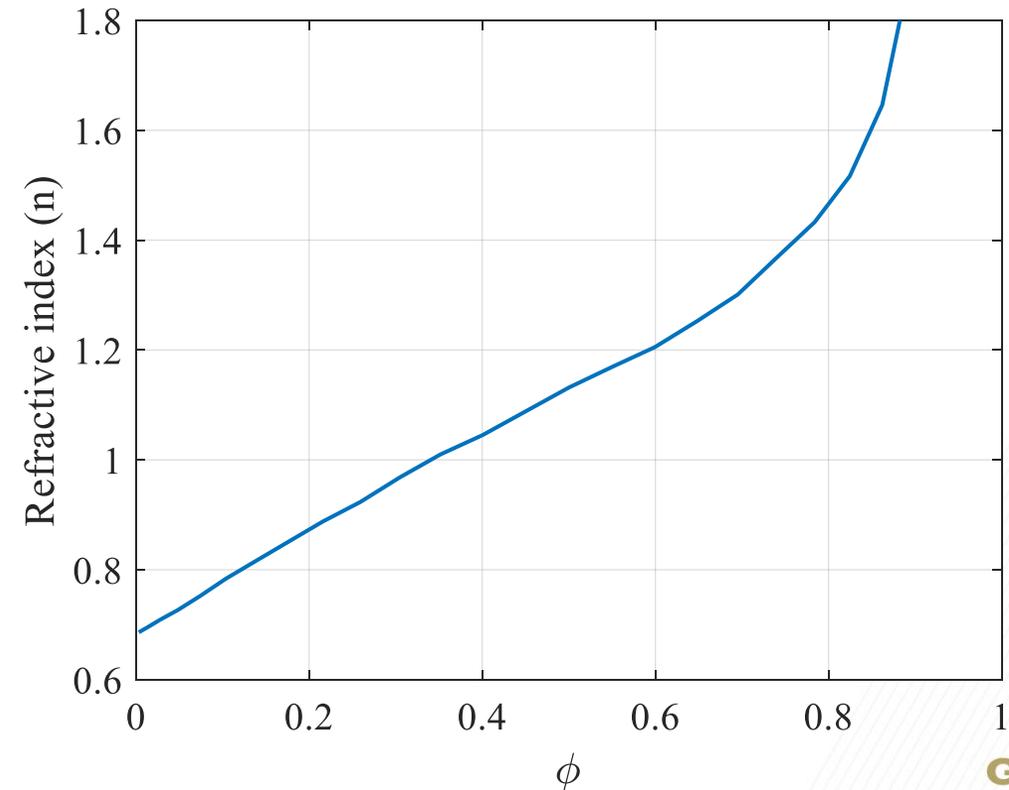
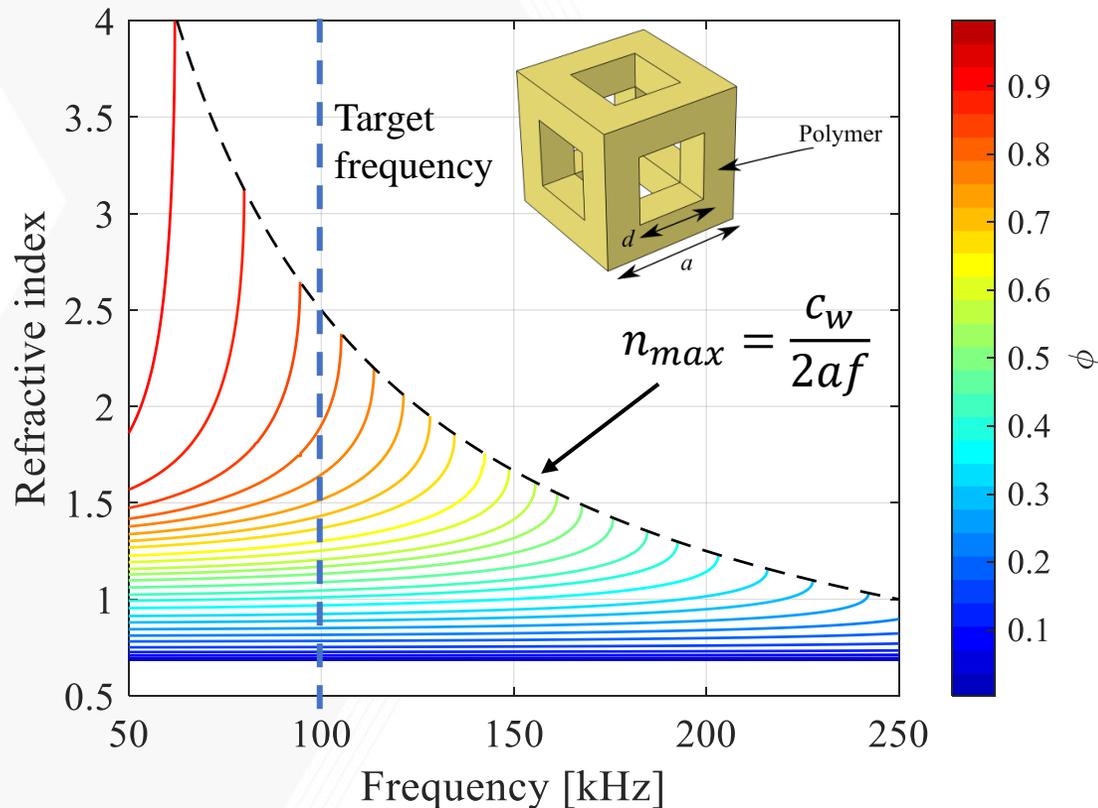
# Effect of inclusion height on the refractive index

- The refractive index of the material ( $n$ ) is given by:

$$n = \frac{c_w}{c_{eff}}$$

$c_w$ : Speed of sound in water

$c_{eff}$ : Effective wave speed in the crystal



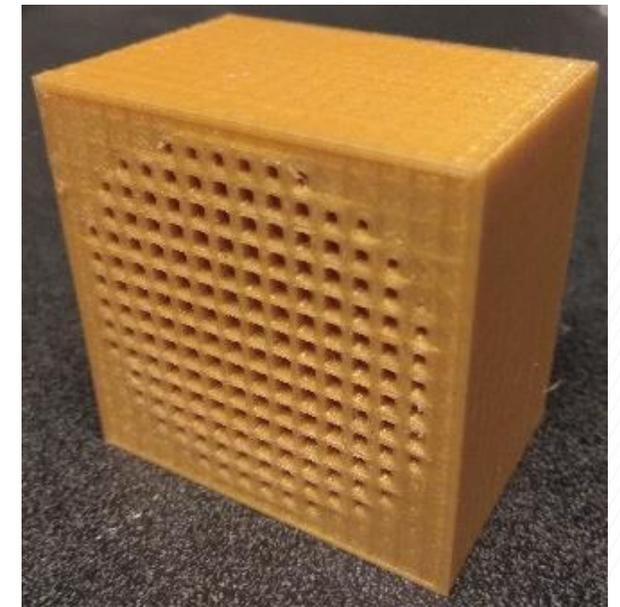
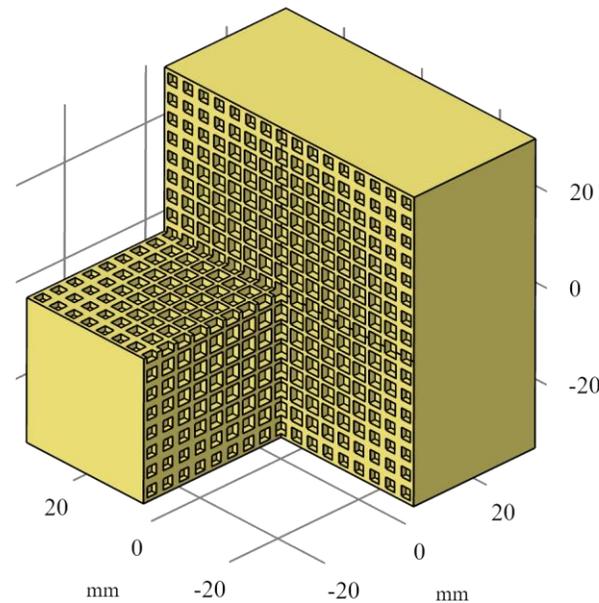
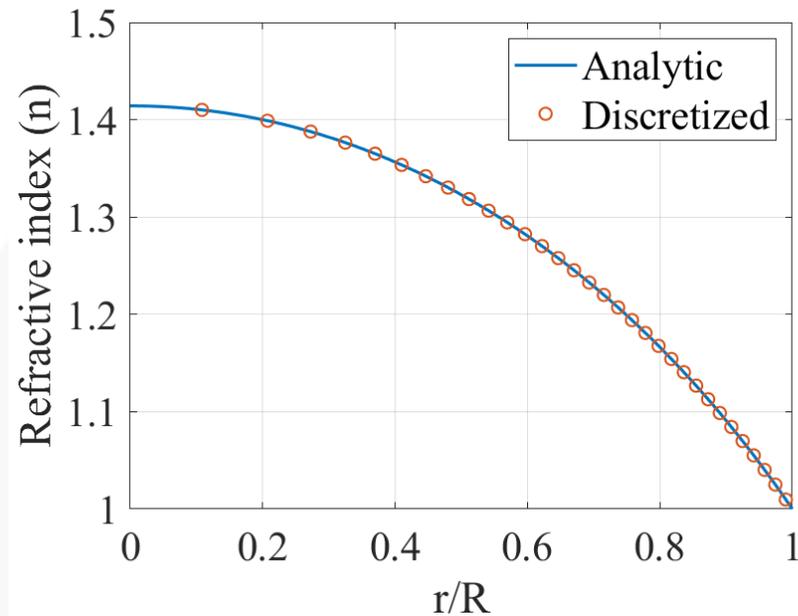
# Luneburg lens in 3D

- Luneburg Lens can be constructed by varying the refractive index of the material gradually in space according to the profile:

$$n(r) = \sqrt{1 - \frac{r^2}{R^2}}$$

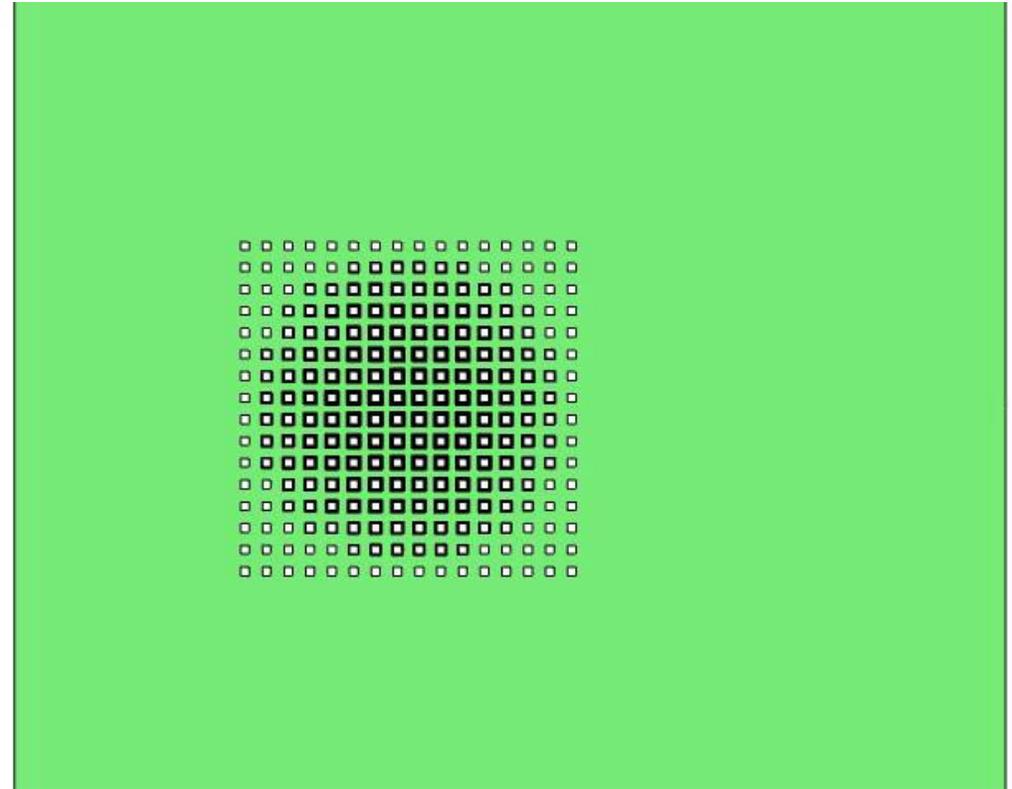
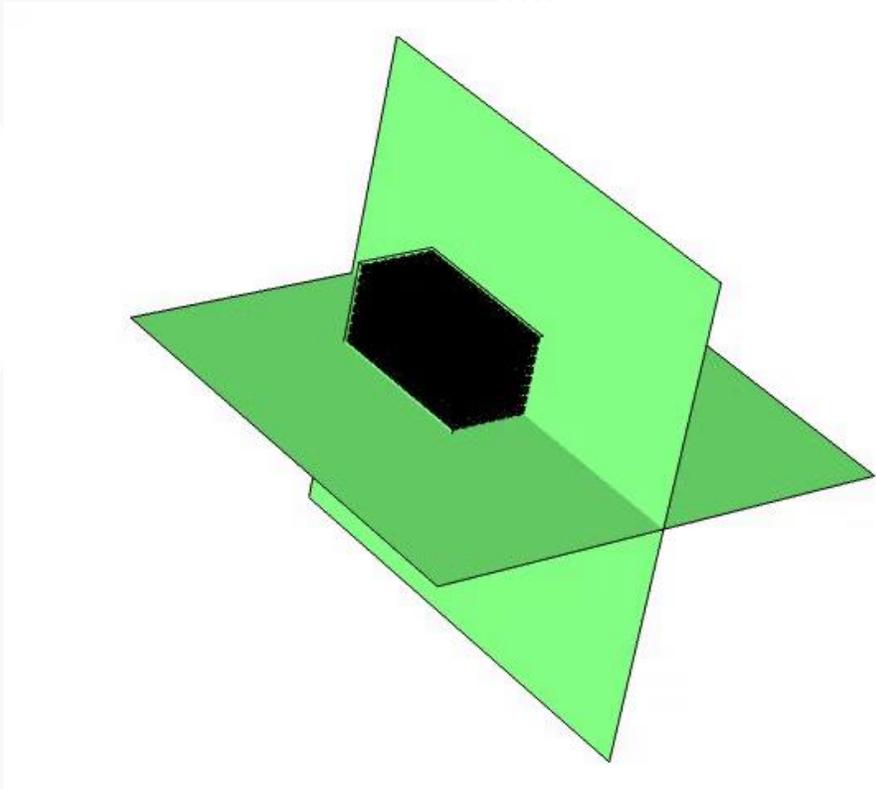
$r$ : position in space

$R$ : radius of the lens



# Time domain numerical model

- A 3D coupled elastic-acoustic FEM model of the lens is simulated in the time domain



# Lens fabrication

- Identified material properties:

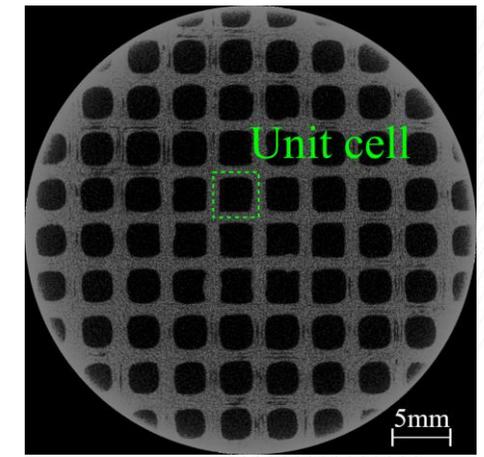
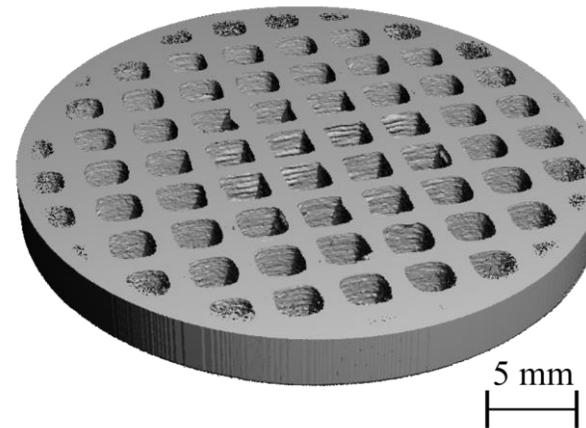
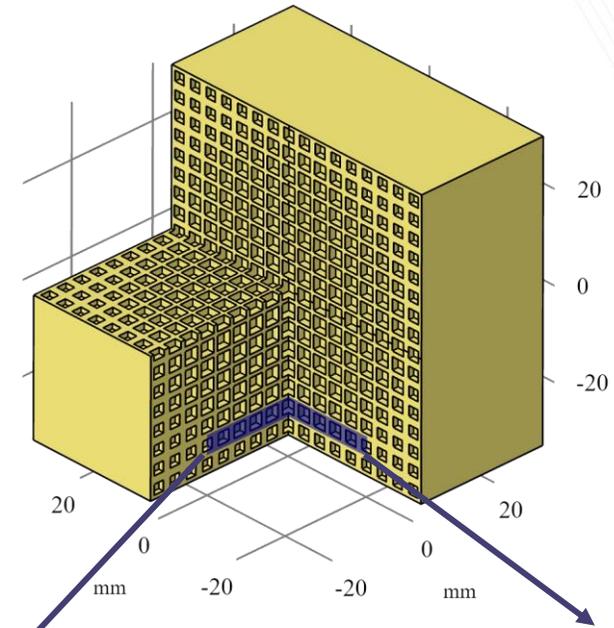
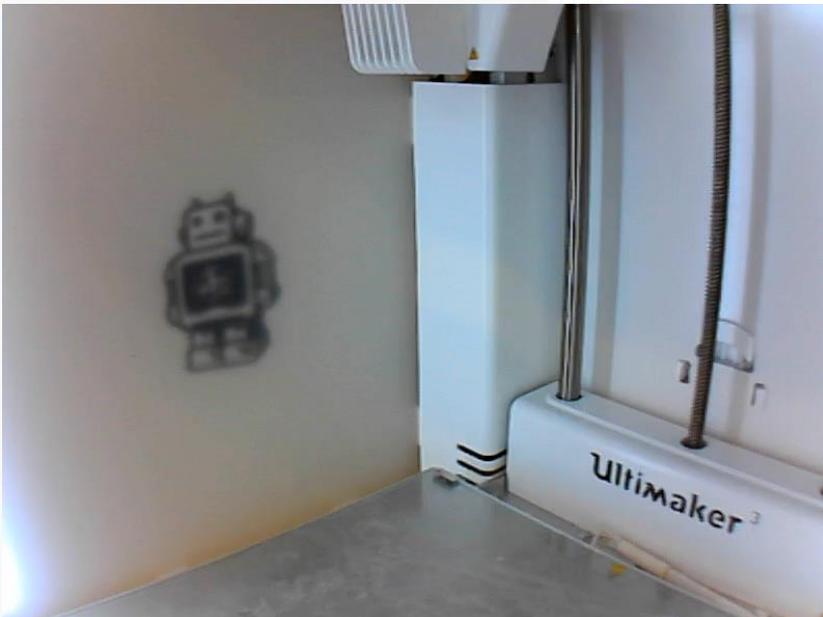
$$E_{PLA} = 3200 \pm 50 \text{ MPa}, \quad \rho_{PLA} = 1117 \text{ kg/m}^3$$
$$\eta_{PLA} = 0.021 \pm 0.003$$

- Unit cell size:  $a = 3 \text{ mm}$
- Lens Dimensions:

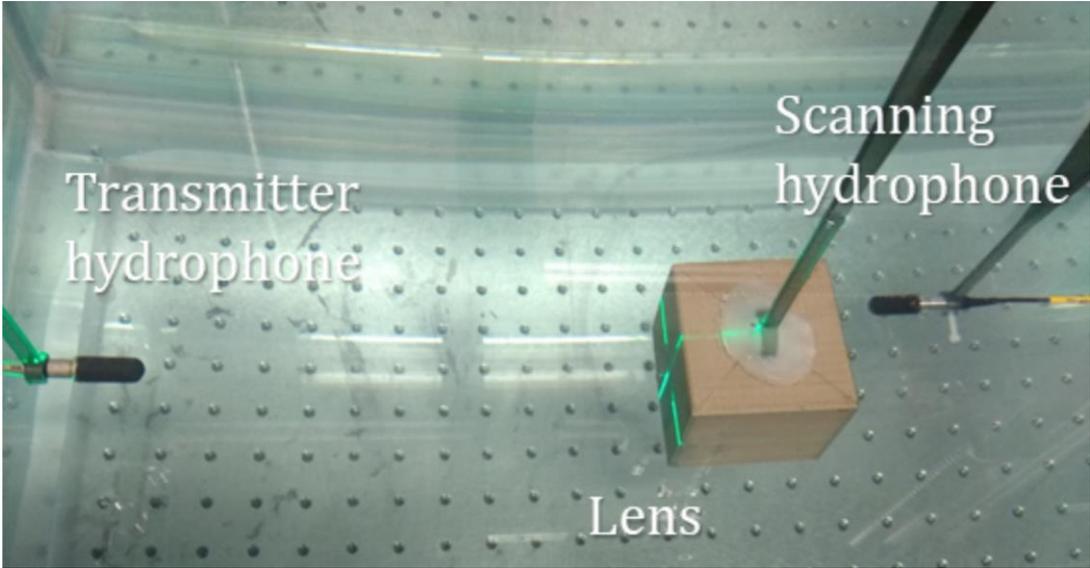
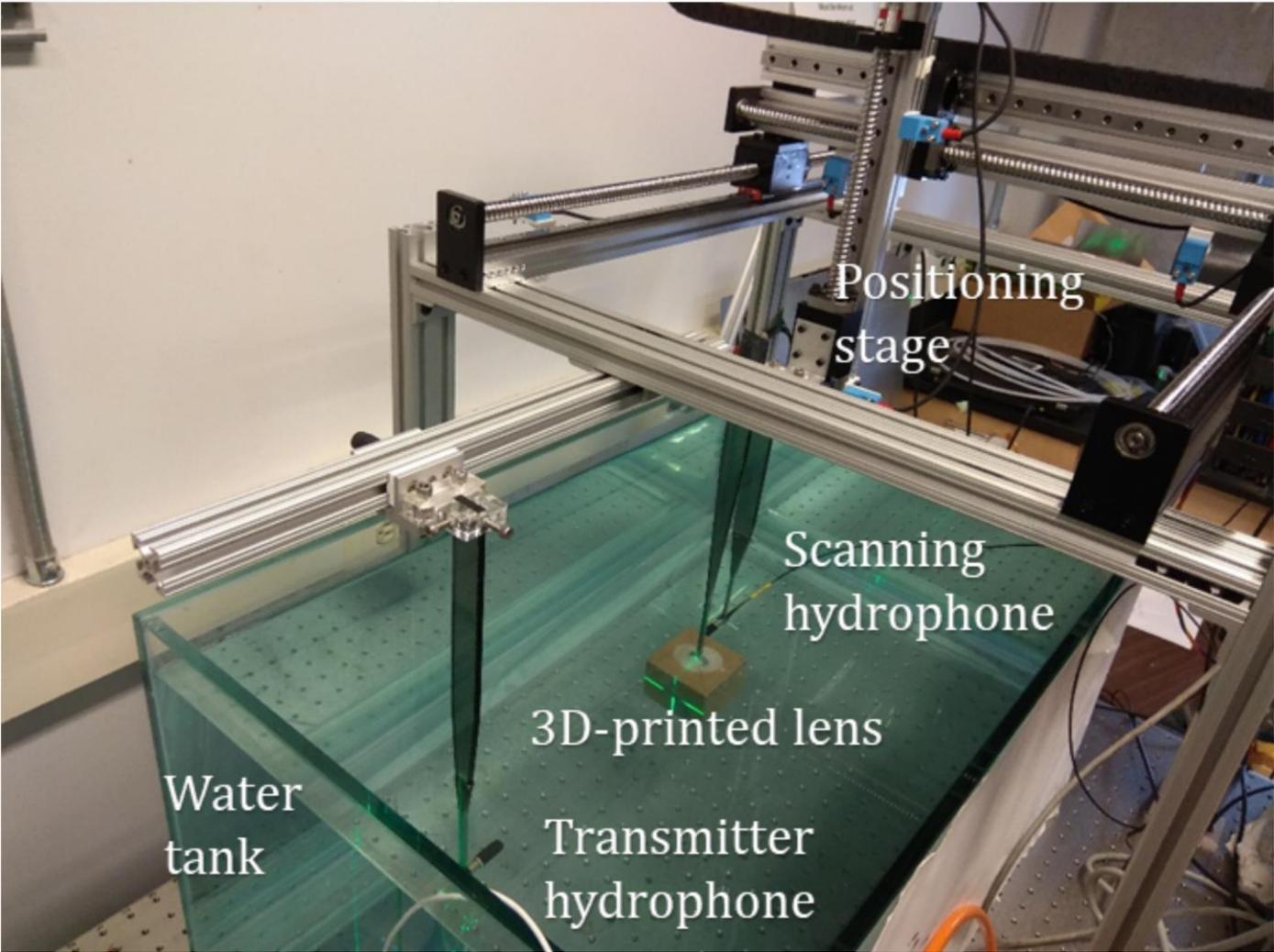
$$16 \text{ cell} \times 16 \text{ cell} \times 16 \text{ cell} = 48 \text{ mm} \times 48 \text{ mm} \times 48 \text{ mm} \sim 3 \lambda$$

- Printing time:

16-40 hours

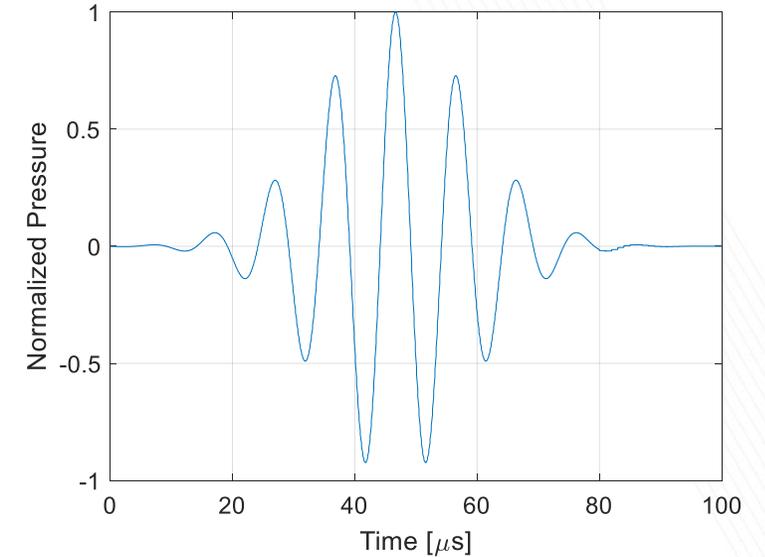


# Experimental setup

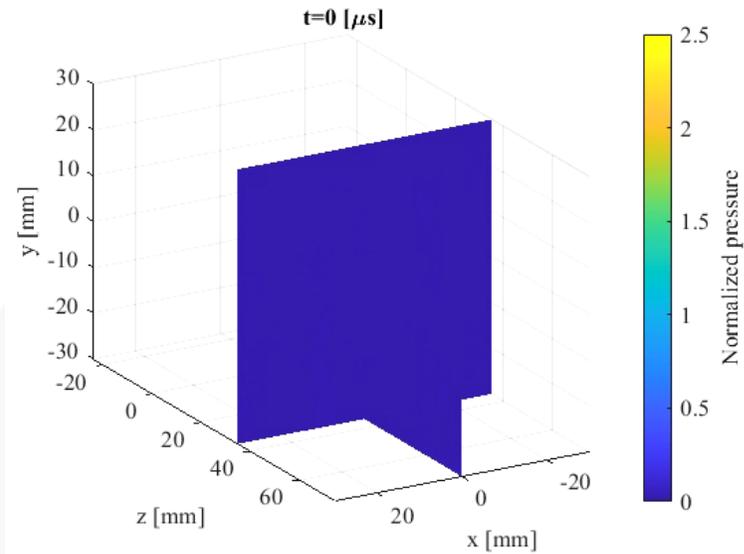


# Lens performance (Time domain)

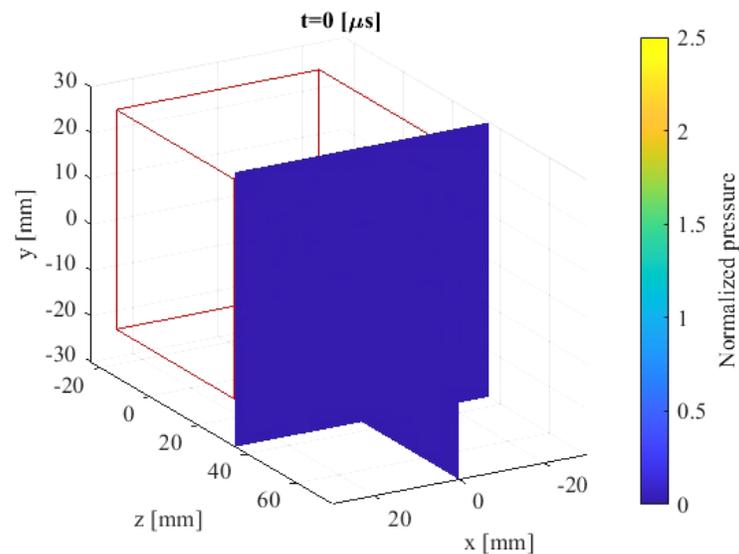
- Exciting the lens with a Gaussian pulse centered at 100 kHz with 30kHz bandwidth



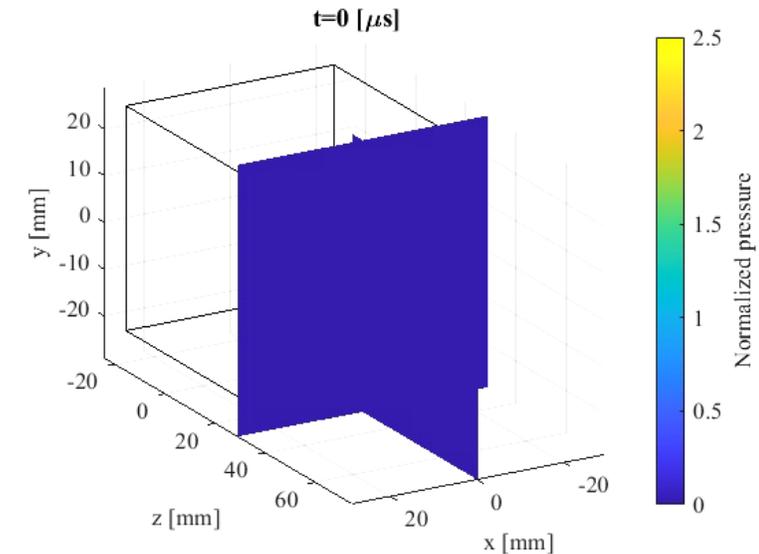
Without lens



Experimental

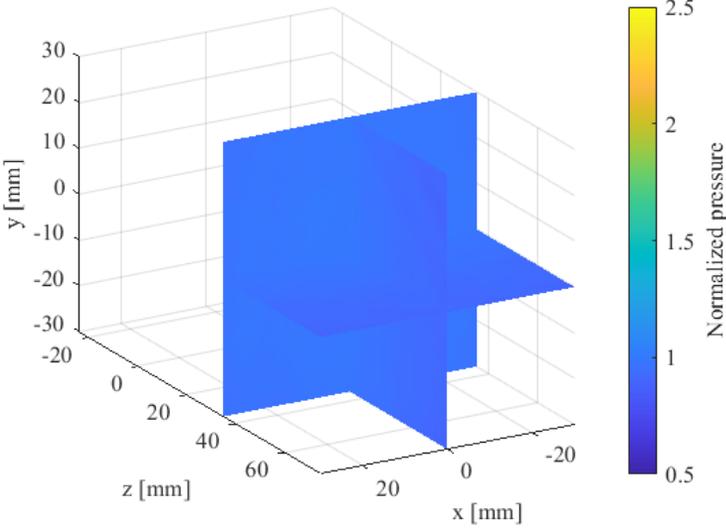


Numerical

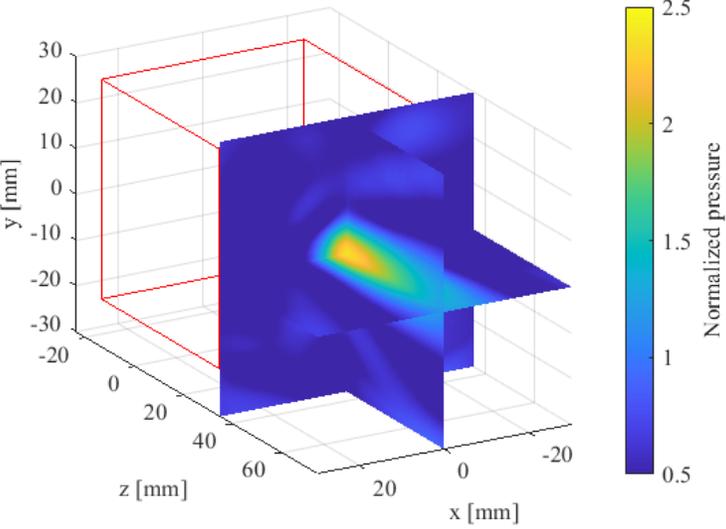


# Lens performance (RMS pressure)

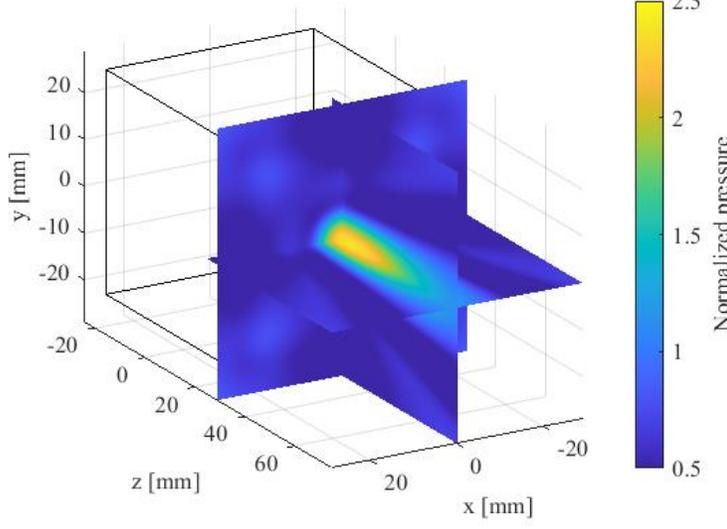
Without lens



Experimental

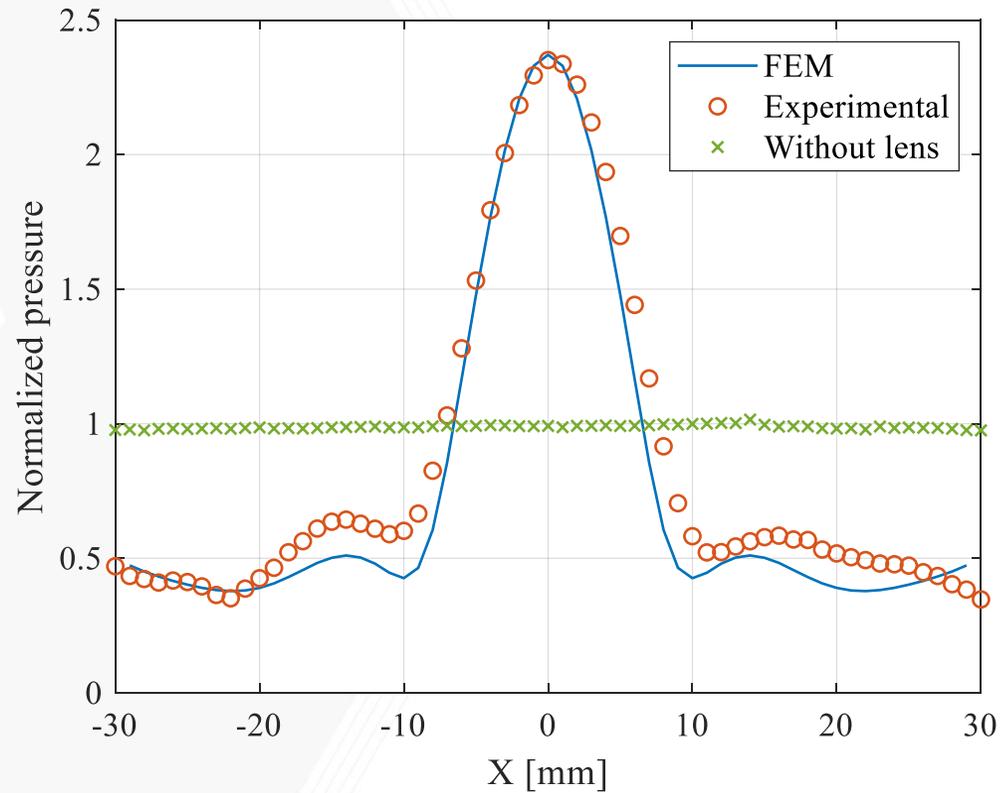


Numerical

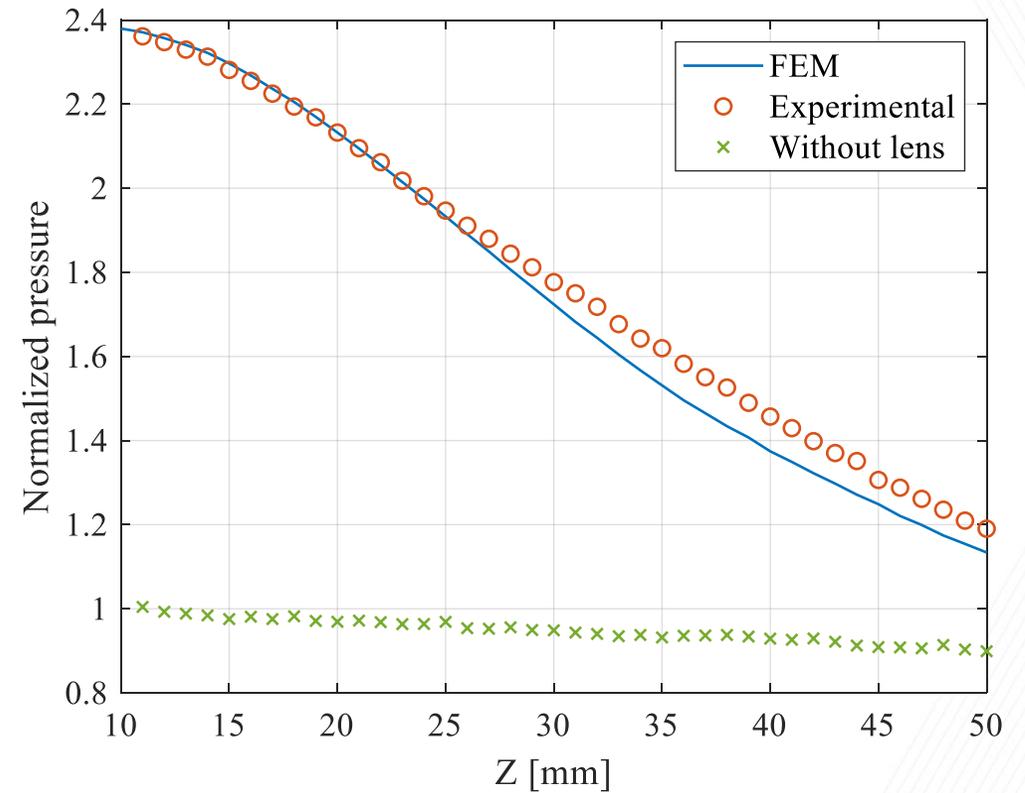


# Lens performance

## Focal plane



## Propagation plane



# Conclusions

- Air inclusions in a polymer matrix phononic crystals can be used to direct ultrasonic waves underwater.
- A novel phononic crystal-based Luneburg lens has been designed, analyzed, 3D-printed, and experimentally validated.
- The realized lens achieves a power gain 8 dB at the focal point.
- The introduced lens can find potential applications in acoustic wireless power harvesting/transfer as well as signal enhancement in underwater sensing.

# Acknowledgment

- This material is based upon work supported by the National Science Foundation under Grant No.(1727951)



**Thanks!..  
Questions?**